

# **Systems biology from simple models to biomarker identifications**

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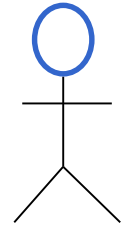
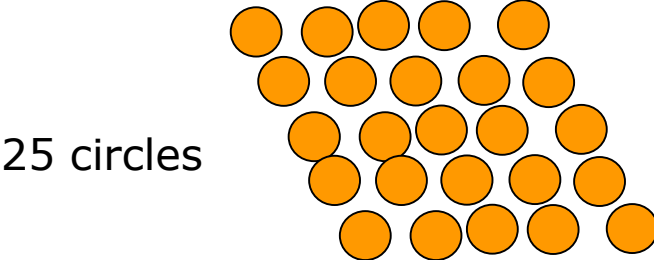
Technical University of Denmark,

Denmark.

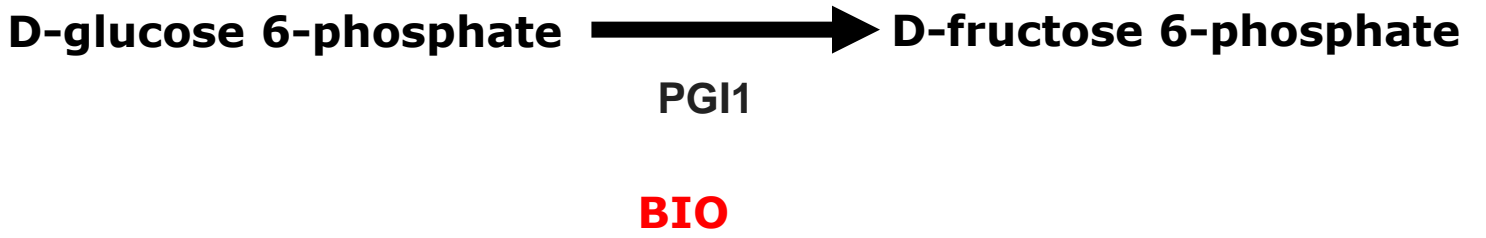
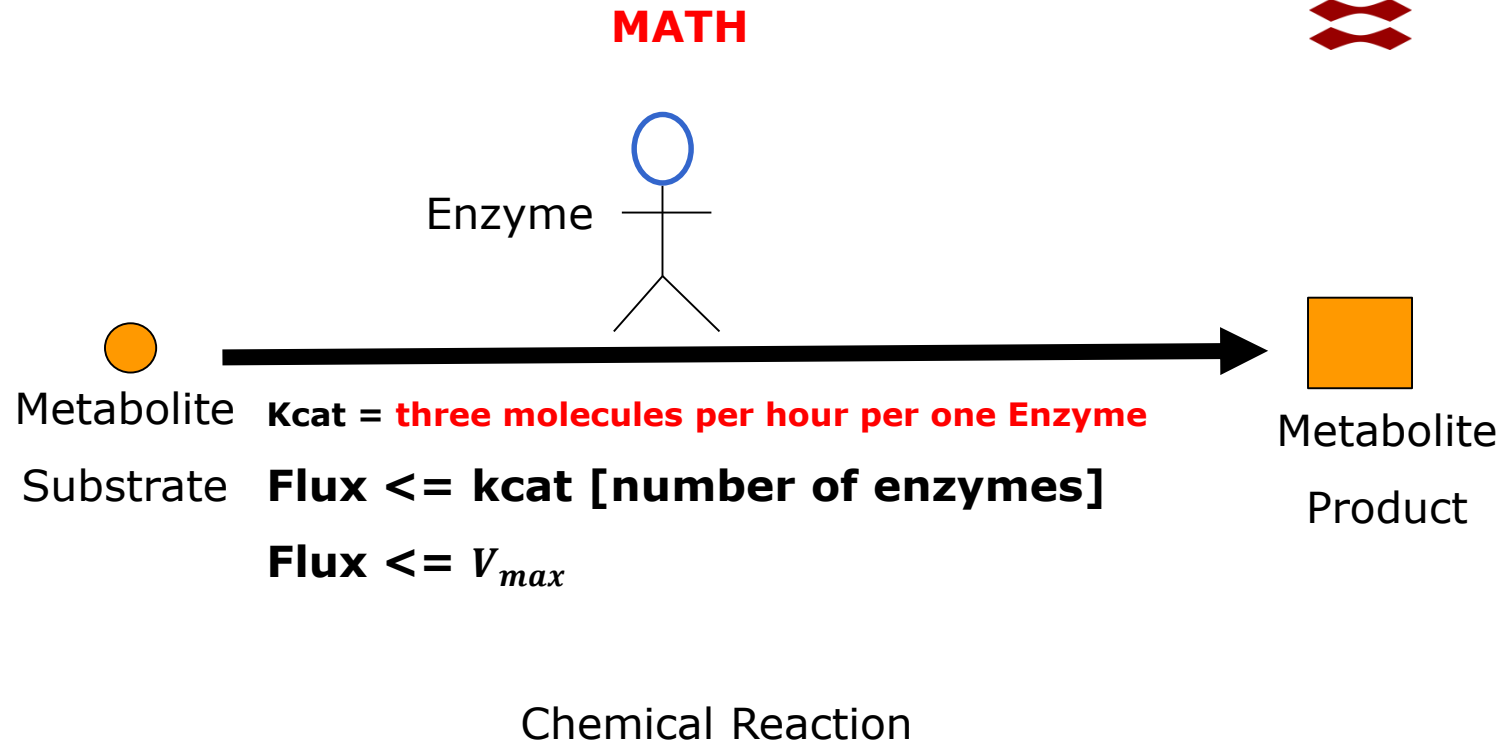
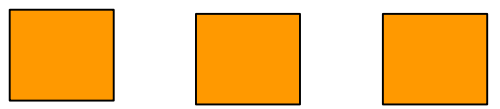
# Outlines

- **What is Systems Biology?**
- **How to cross the bridge from math to biology or from biology to math?**
- **How to build a simple model?**
- **How to analyze RNA-seq data and integrate the results with a simple model?**
- **How to identify new biomarkers?**
- **Can we build a whole-cell model?**

# Simple Problem

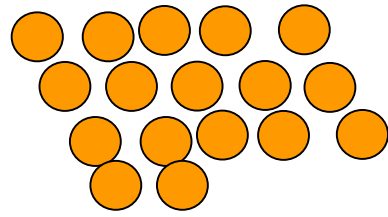


Converts **three circles** to square **per hour**



Q. How many circles remain **after two hours**?

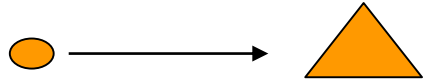
A. This man can convert 6 circles after two hours, so there are 19 circle after two hours.



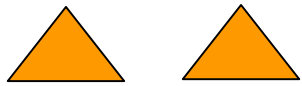
17 circles



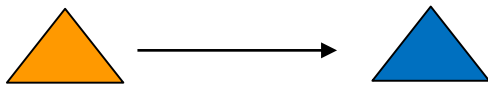
Converts three 1 circles to triangle per hour



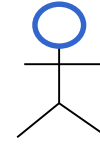
How many triangles can this man moves after two hours?



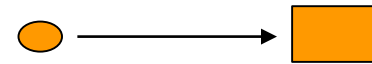
Changes color of 0.5 triangle to blue per hour



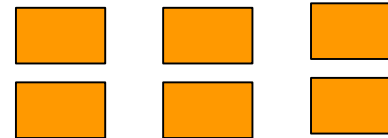
How many triangle can this man change after two hours?



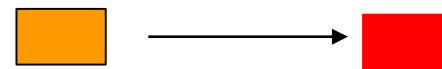
Converts three circles to square per hour



How many squares can this man convert after two hours?



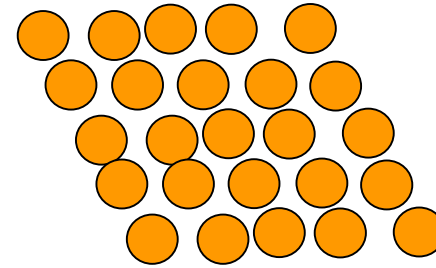
Changes color of two squares to red red per hour



How many red squares can this man convert after two hours?

# Mathematical Modeling

So If we have 25 circles



How many objects do we have after two hours

We can also estimate the wait time?

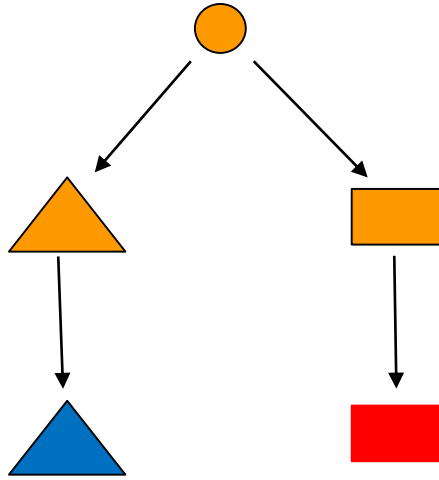


17  
2  
4  
1

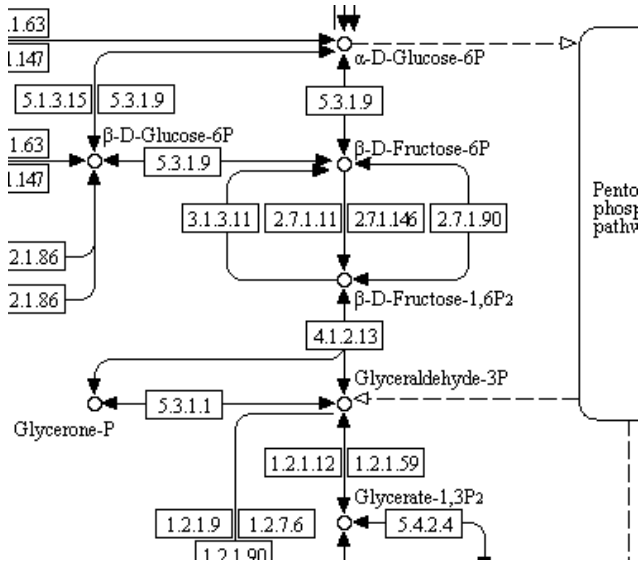


1  
1  
1  
1

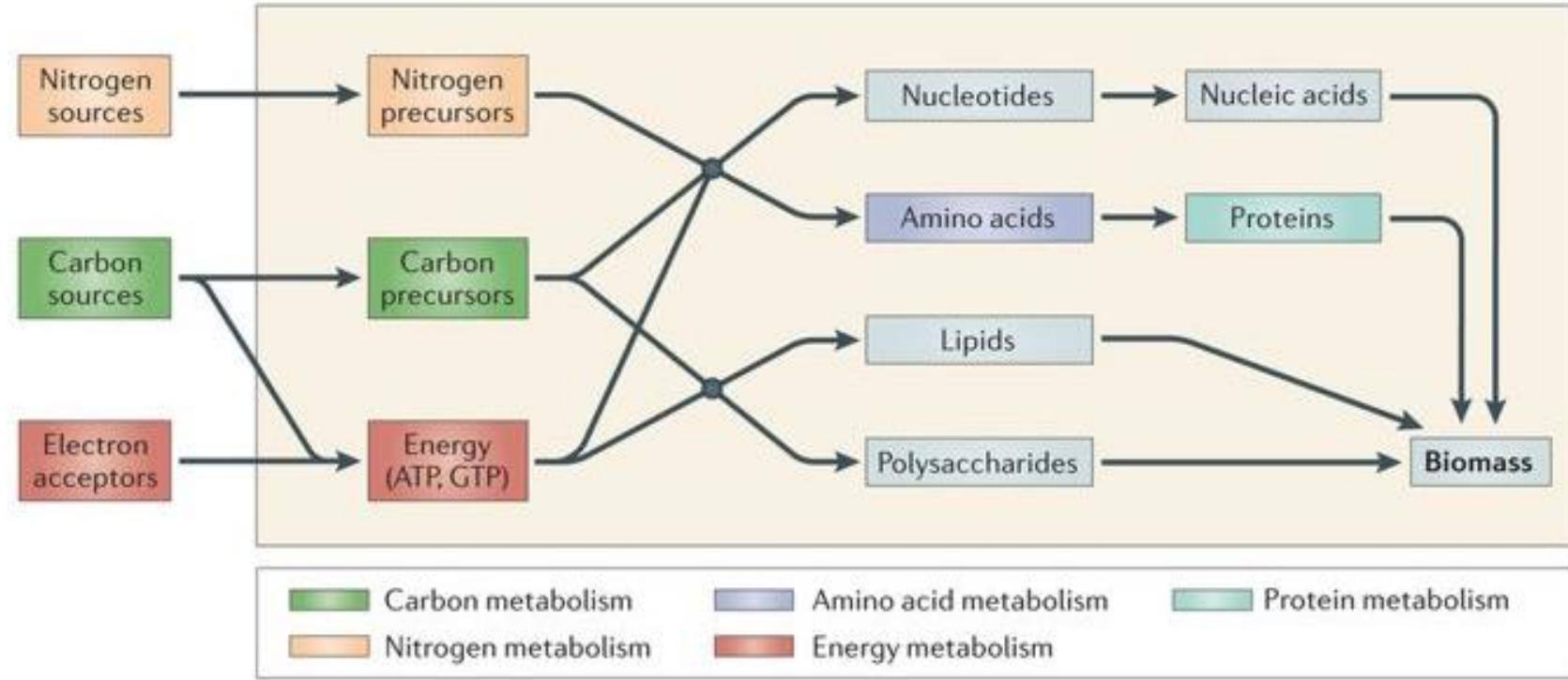
# MATH



# Pathway



# Bio

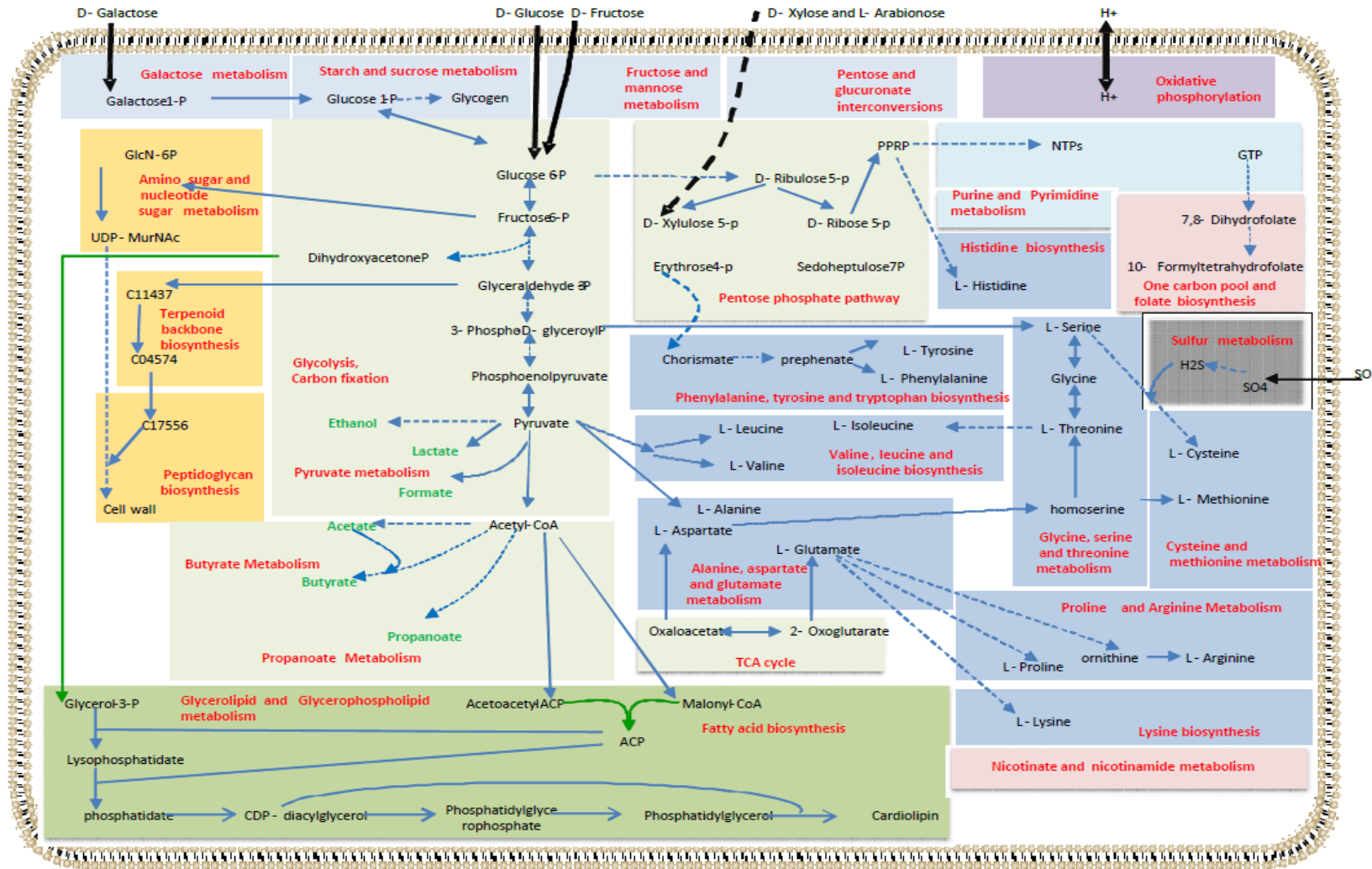


[Nat Rev Microbiol.](#) 2014 May;12(5):327-40.

**We can estimate how many copies of nucleotides, amino acids, lipid species, and carbohydrates per cell**

Biomass Reaction

# Genome-Scale Metabolic Models



If we know the uptake rate of glucose,  
Can we estimate the growth rate?

For example,

yeast can consume glucose with the rate  $13 * 6.023 * 10^8$  molecules per cell per hour,

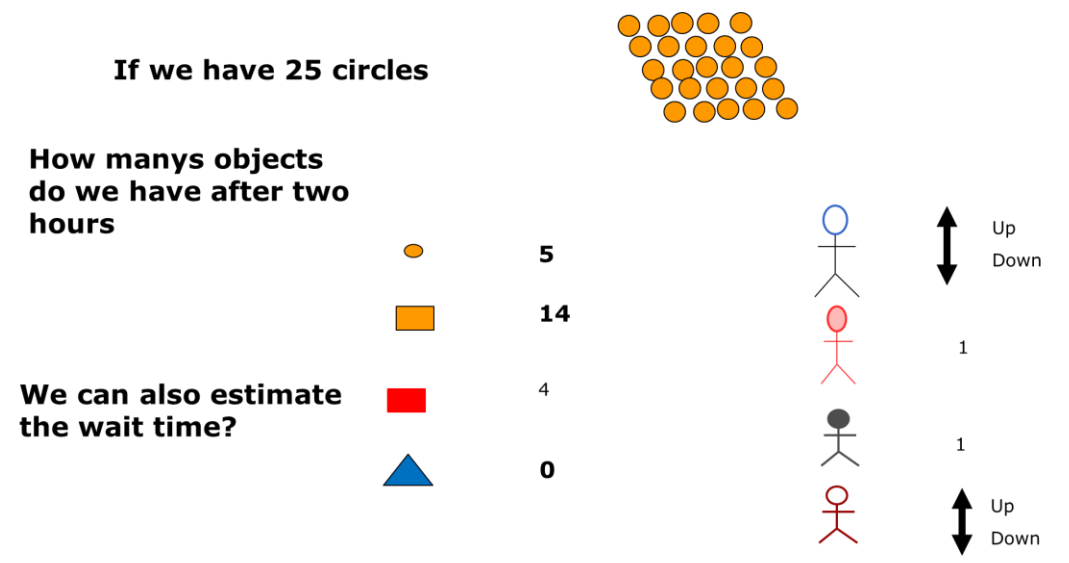
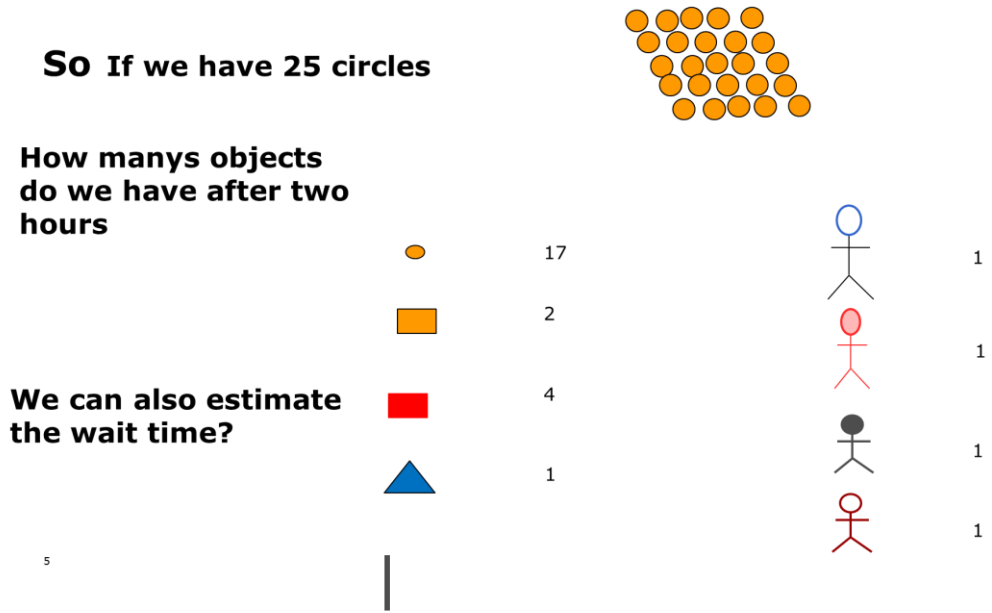
We know the copies numbers of nucleotides, amino acids, lipid species, and carbohydrates per yeast cell

The growth rate is 0.1 per hour

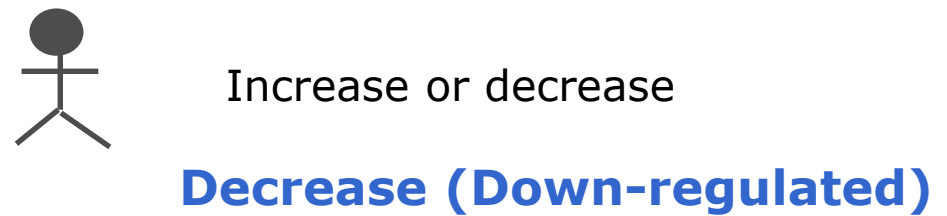
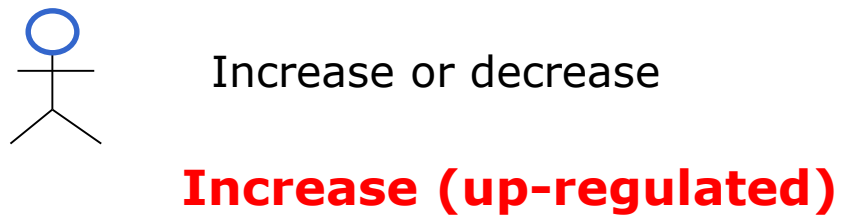
# Quantitative description (Proteomics and Metabolomics)

## Condition1 (normal or WT)

## Condition2 (Disease or mutant)



Please note the change in number of Circles and Squares.



# Formal Definition of Systems Biology

- to obtain new insight into the molecular mechanisms occurring in living cells or sub-systems of living cells, through the combination of **mathematical modeling** and **experimental biology** and
- to obtain a **quantitative description of biological systems** in the form of mathematical models that can be used for predictive analysis.

## Mathematical Modeling

Math:  
 Linear programming

Physics:  
 Thermodynamics,

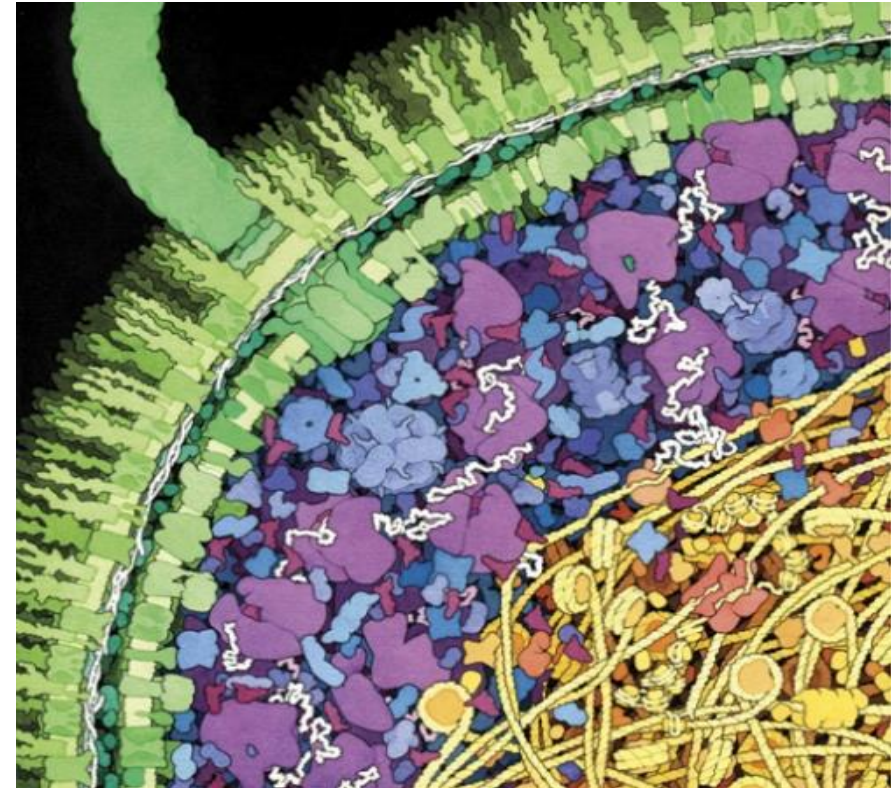
## Experimental biology

Fermentation  
 Enzyme Kinetics  
 13C flux

## Quantitative description

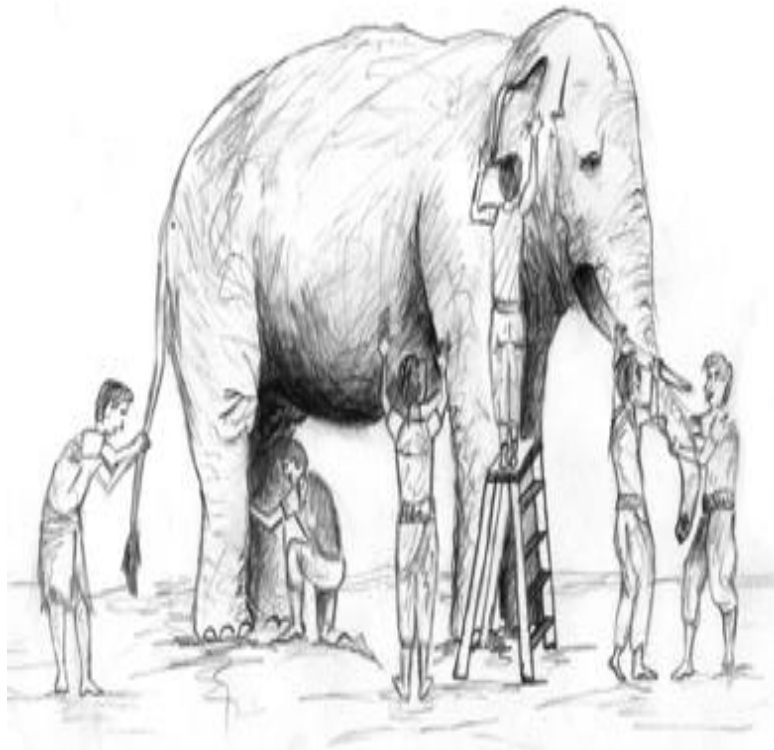
Genomics,  
 RNA-seq,  
 Proteomics  
 Metabolomics

# What is the aim of the Systems Biology?

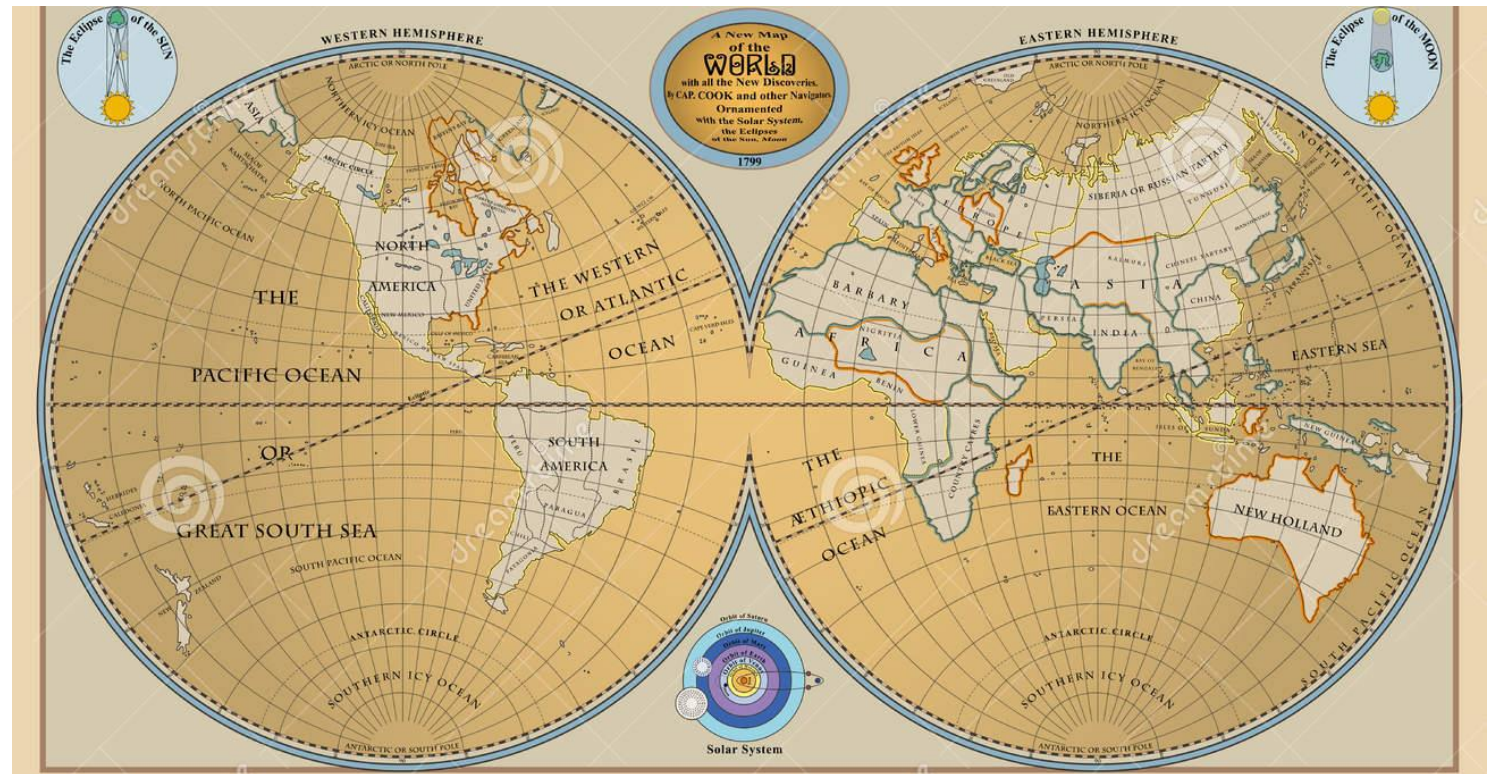


**The aim is to find the cellular components and how these components are connected together.**

# We need genome-scale methods not small models



<http://www.biokemi.org/biozoom/issues/514/articles/2285>



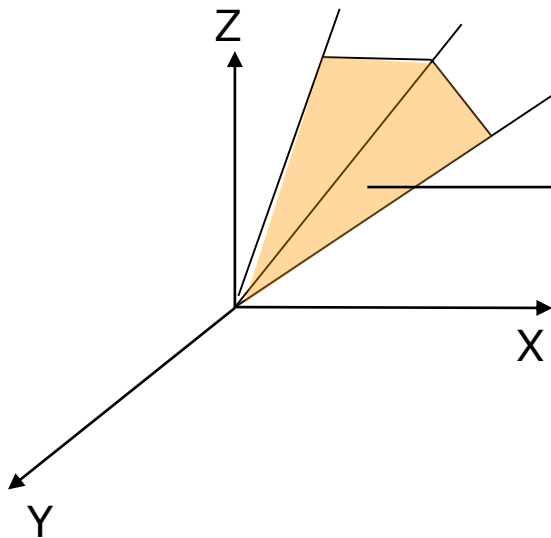
<https://www.dreamstime.com/stock-illustration-vector-old-globe-map-world-new-discoveries-image60583134>

# Math Background (Linear programming)

$$\begin{aligned}
 x + y - z &= 0 \\
 x - y - z &= 0, \\
 x, y, z &\geq 0
 \end{aligned}$$



$$\begin{matrix} S & v & = & 0 \\
 \begin{bmatrix} 1 & 1 & -1 \\ 1 & -1 & -1 \end{bmatrix} & \begin{bmatrix} x \\ y \\ z \end{bmatrix} & = & \begin{bmatrix} 0 \\ 0 \end{bmatrix}
 \end{matrix}$$



Solution space  
each point is a solution  
for this system

**We can use the computer to solve this problem**

**The problem we need a point that maximizes z**

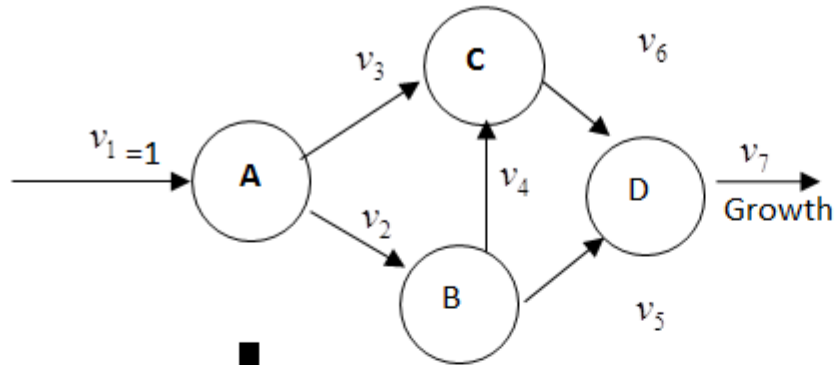
**Max z**

***s.t.***

$$S v = 0,$$

$$0 \leq v \leq 100$$

# Simulation: Flux balance analysis



$$\text{Max Growth} = v_7$$

s.t.

$$SV = 0$$

$$-100 \leq v_i \leq 100,$$

$$v_1 = 1$$

$$\begin{aligned} \frac{dA}{dt} &= v_1 - v_2 - v_3 = 0 \\ \frac{dB}{dt} &= v_2 - v_4 - v_5 = 0 \\ \frac{dC}{dt} &= v_3 + v_4 - v_6 = 0 \\ \frac{dD}{dt} &= v_5 + v_6 - v_7 = 0 \end{aligned}$$



$$\begin{bmatrix} \frac{dA}{dt} \\ \frac{dB}{dt} \\ \frac{dC}{dt} \\ \frac{dD}{dt} \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_6 \\ v_7 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

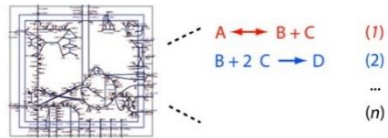
**Stoichiometric Matrix  $S$**



# What is Flux Balance Analysis (FBA)

## Chemical reactions

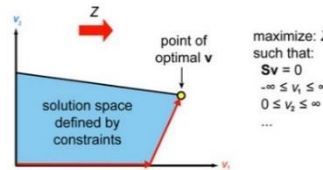
a Curate metabolic reactions



c Apply mass balance constraints

$$S \begin{matrix} (m \times n) \\ \begin{matrix} -1 & 1 & 1 \\ 1 & -1 & -2 \\ 1 & -2 & 1 \\ \dots & \dots & \dots \end{matrix} \end{matrix} * \begin{matrix} v \quad (n \times 1) \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ \dots \end{matrix} \end{matrix} = 0 \rightarrow \begin{matrix} m \text{ mass balance} \\ \text{equations} \\ -v_1 + \dots = 0 \\ v_1 - v_2 + \dots = 0 \\ v_1 - 2v_2 + \dots = 0 \\ v_2 + \dots = 0 \\ \dots \end{matrix}$$

e Optimize Z using linear programming



b Formulate S matrix

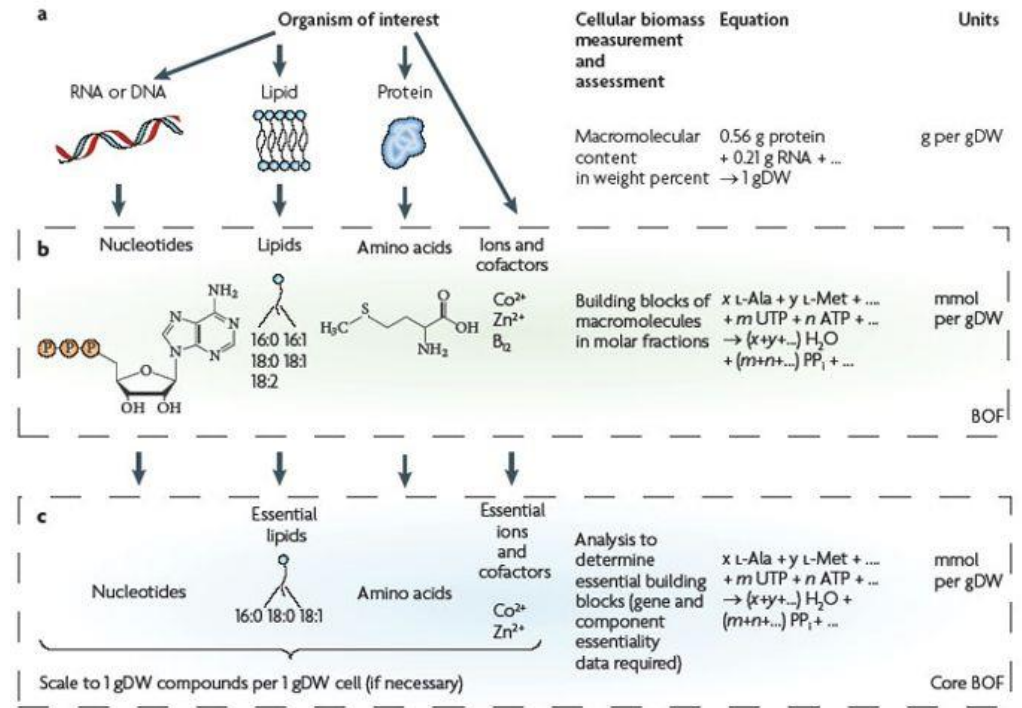
		Reactions			
		1	2	...	n
Metabolites	A	-1			
	B	1	-1		
	C	1	-2		
	D			1	
	...				
...					
m					

d Define objective function Z

$$Z = \begin{matrix} c^T \quad (1 \times n) \\ \begin{matrix} 1 & 0 & \dots & 0 \end{matrix} \end{matrix} * \begin{matrix} v \quad (n \times 1) \\ \begin{matrix} v_1 \\ v_2 \\ \dots \\ v_n \end{matrix} \end{matrix}$$

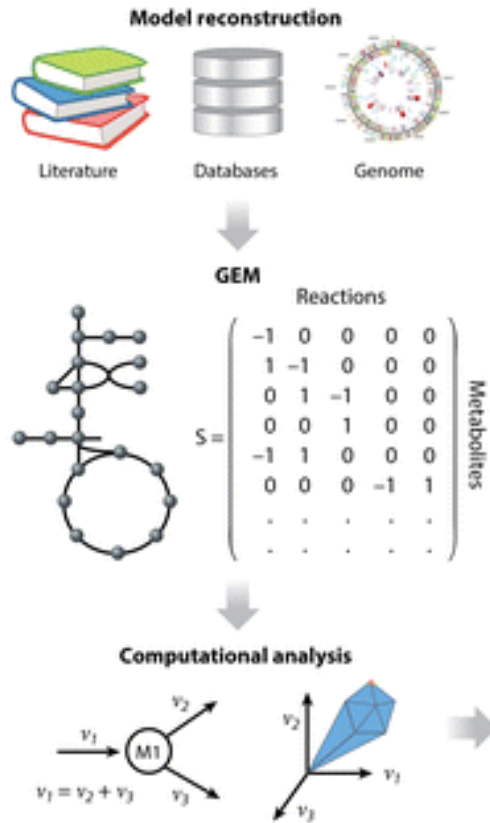
sets reaction 1 as the objective

## Biomass reaction



Nature Reviews | Microbiology

# How can you reconstruct the model



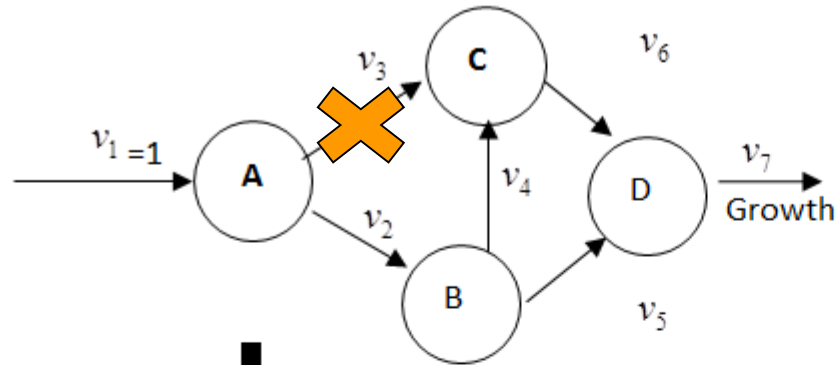
Reaction	Genes
$S1 + S2 \rightarrow P1 + P2$	g1
$S1 + S3 \rightarrow P3 + P4$	g1 and g2
$S3 \rightarrow P5$	g1 or g3
...	...

Please remember this rule:

- You input the glucose uptake rate as 1 mmol/gDW/h
- FBA maximizes the growth rate
- The model predicts the growth rate

Nielsen J. 2017. Annu. Rev. Biochem. 86:245–75

# Simulation: Flux balance analysis



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s.t.

$$SV = 0$$

$$-100 \leq v_i \leq 100,$$

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$$\begin{aligned} \frac{dA}{dt} &= v_1 - v_2 - v_3 = 0 \\ \frac{dB}{dt} &= v_2 - v_4 - v_5 = 0 \\ \frac{dC}{dt} &= v_3 + v_4 - v_6 = 0 \\ \frac{dD}{dt} &= v_3 + v_5 - v_7 = 0 \end{aligned}$$



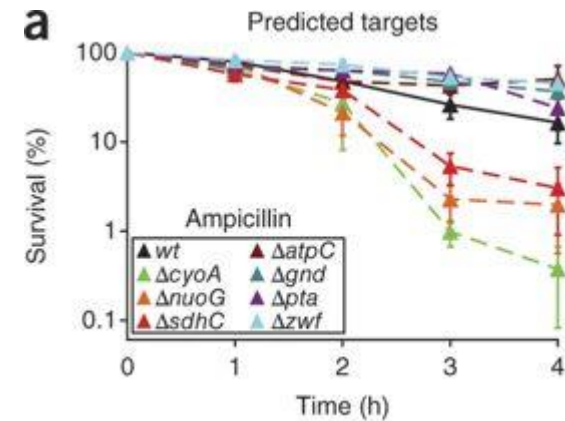
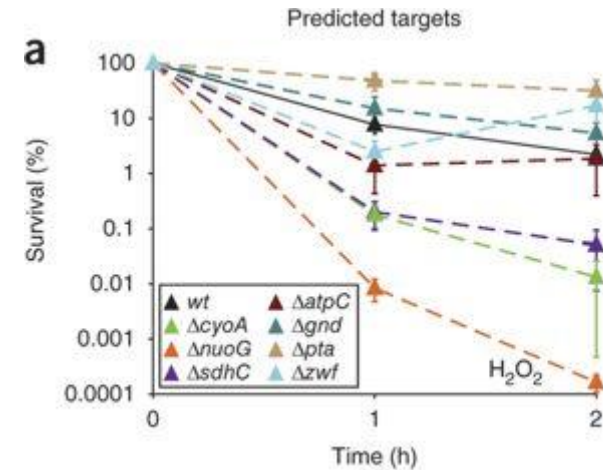
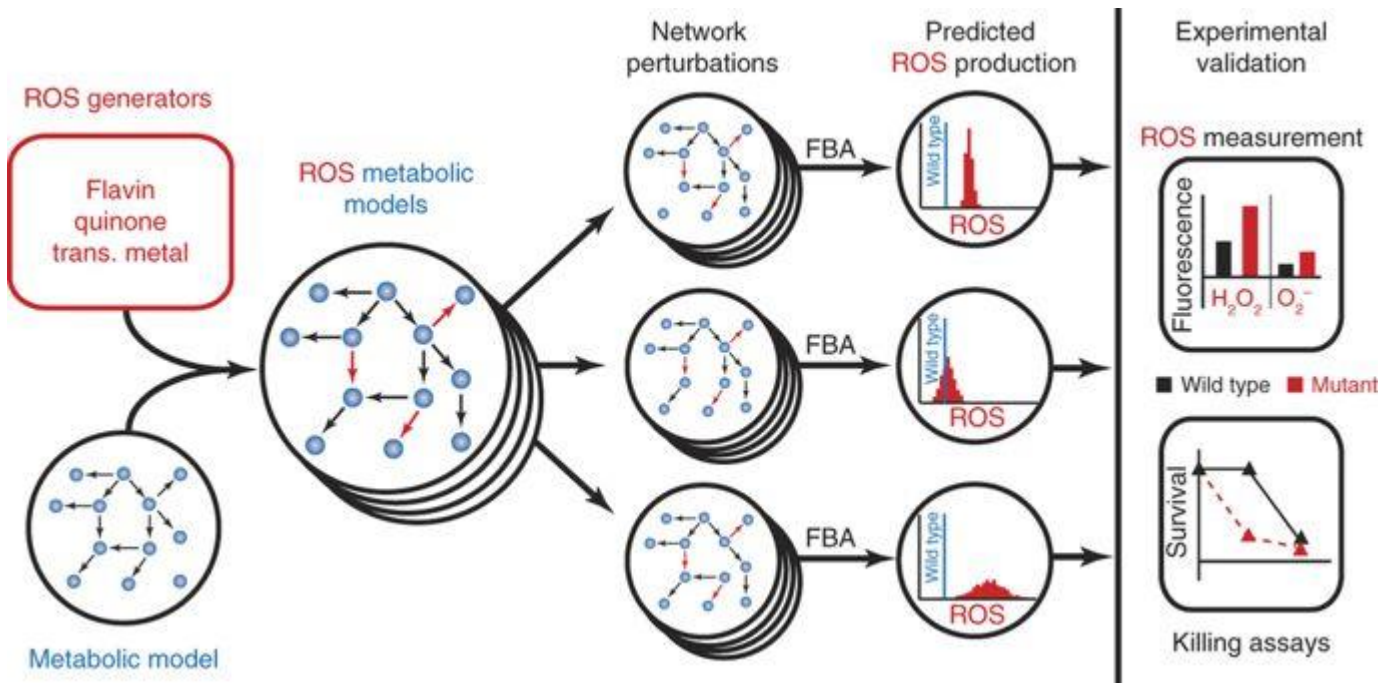
$$\begin{bmatrix} \frac{dA}{dt} \\ \frac{dB}{dt} \\ \frac{dC}{dt} \\ \frac{dD}{dt} \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_6 \\ v_7 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Stoichiometric Matrix  $S$



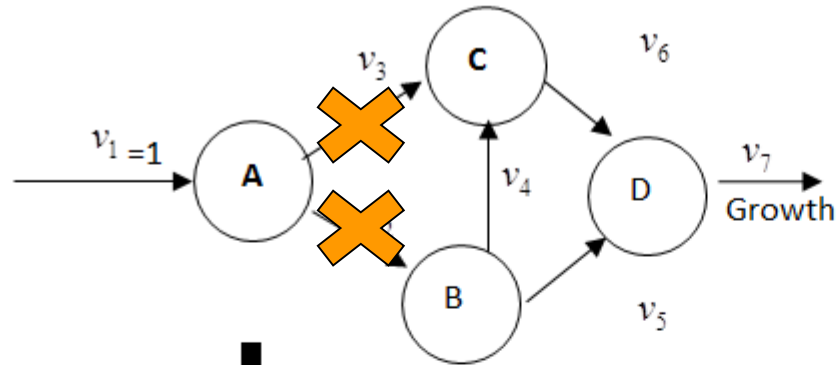
# Finding antibiotics (deleting one reaction or gene)

Reactive oxygen species (ROS) such as H<sub>2</sub>O<sub>2</sub> can kill bacteria, can we attack the resistance mechanism in bacteria



Nature Biotechnology volume 31, pages 160–165 (2013)

# Simulation: Flux balance analysis



$$\text{Max Growth} = v_7$$

s.t.

$$SV = 0$$

$$-100 \leq v_i \leq 100,$$

$$v_1 = 1$$

$$\frac{dA}{dt} = v_1 - v_2 - v_3 = 0$$

$$\frac{dB}{dt} = v_2 - v_4 - v_5 = 0$$

$$\frac{dC}{dt} = v_3 + v_4 - v_6 = 0$$

$$\frac{dD}{dt} = v_5 + v_6 - v_7 = 0$$

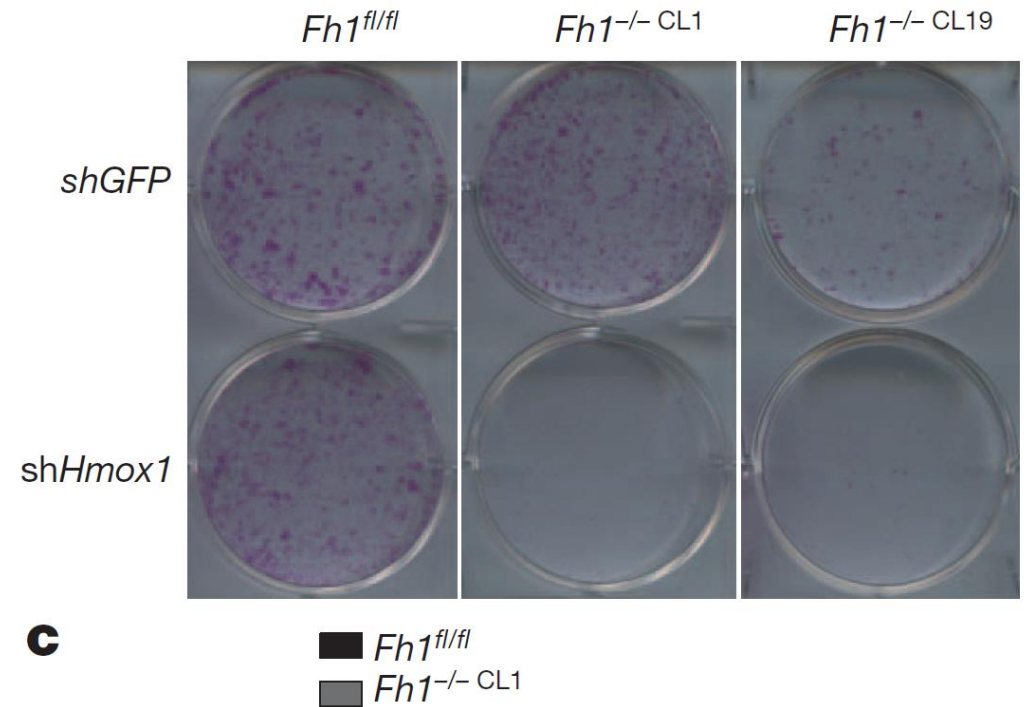
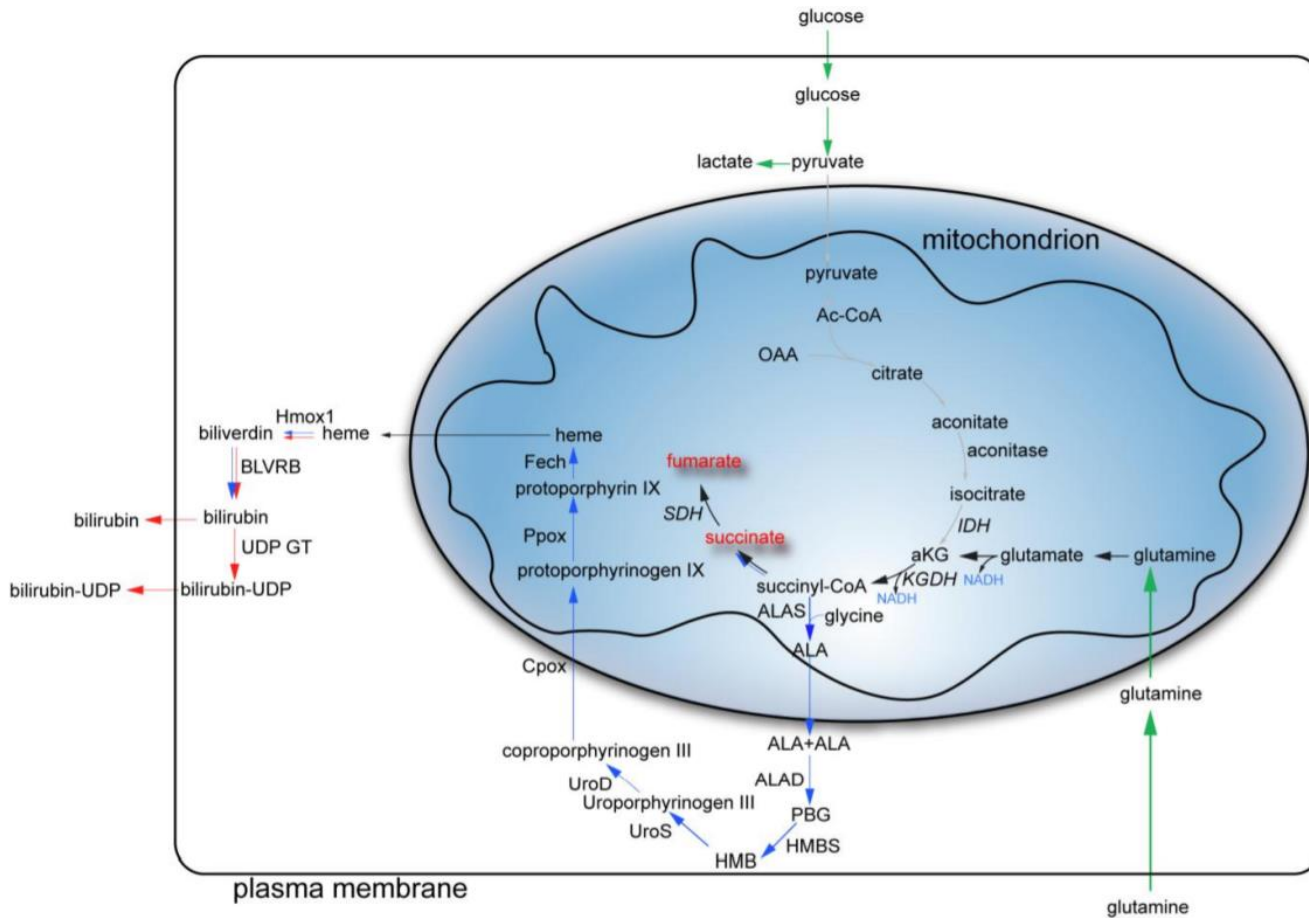


$$\begin{bmatrix} \frac{dA}{dt} \\ \frac{dB}{dt} \\ \frac{dC}{dt} \\ \frac{dD}{dt} \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_6 \\ v_7 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Stoichiometric Matrix  $S$



# GEM Applications: Deleting one reaction (gene)

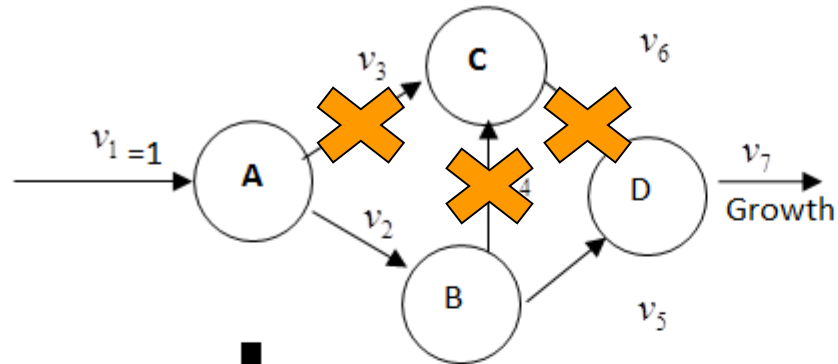


**C**

*Fh1<sup>fl/fl</sup>*  
 *Fh1<sup>-/-</sup> CL1*

*Nature* volume 477, pages 225–228 (08 September 2011)

# Anti-metabolites: Deleting all reactions around one metabolite



$$\text{Max Growth} = v_7$$

s.t.

$$SV = 0$$

$$-100 \leq V \leq 100,$$

$$v_1 = 1$$

$$\frac{dA}{dt} = v_1 - v_2 - v_3 = 0$$

$$\frac{dB}{dt} = v_2 - v_4 - v_5 = 0$$

$$\frac{dC}{dt} = v_3 + v_4 - v_6 = 0$$

$$\frac{dD}{dt} = v_3 + v_5 - v_7 = 0$$



$$\begin{bmatrix} \frac{dA}{dt} \\ \frac{dB}{dt} \\ \frac{dC}{dt} \\ \frac{dD}{dt} \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_6 \\ v_7 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

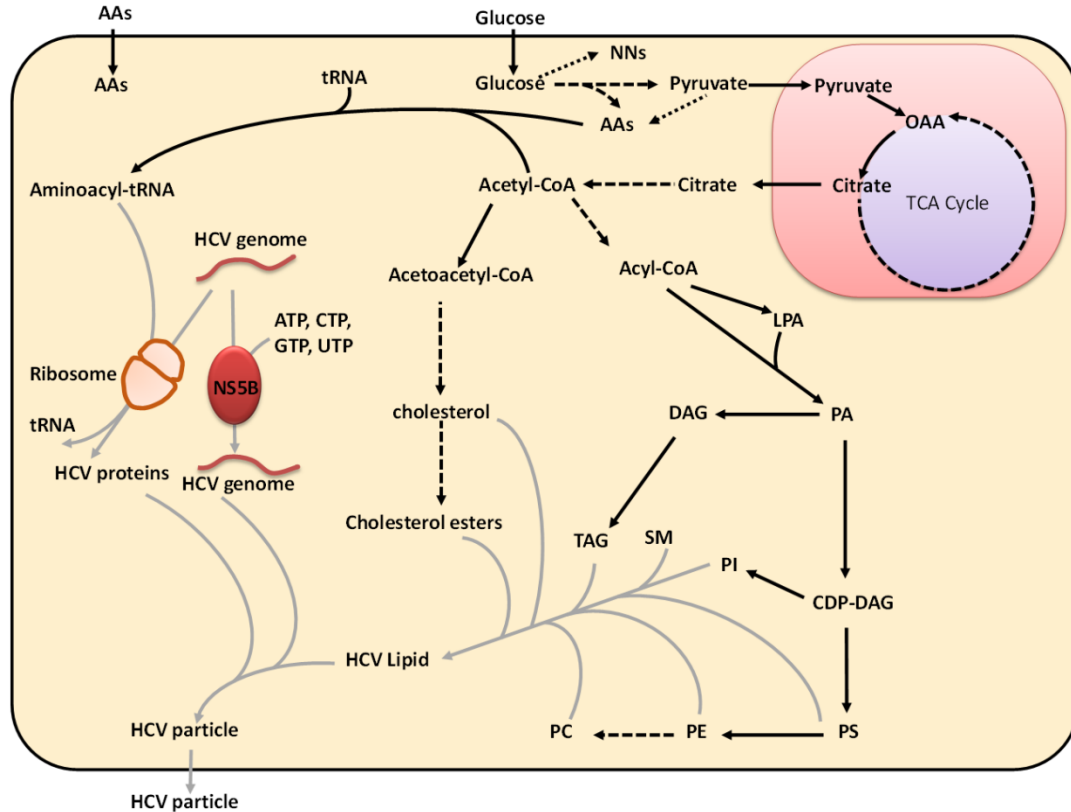
Stoichiometric Matrix  $S$





# HCV

A



Host-targets	Summary	Ref
Acyl-CoA	Liefhebber et al downregulated the acyl-CoA synthetase long-chain family member 1 gene to reduce HCV assembly.	(3)
Acyl-glycerol		
cholesterol esters		
(R)-5-diphosphomevalonate	Jin Ye reviewed the role of mevalonate pathway in HCV assembly.	(4)
(R)-5-phosphomevalonate		
(R)-mevalonate		
Presqualene-PP	Saito et al downregulated the squalene synthase gene to reduce HCV assembly.	(5)
Squalene		
Squalene 2,3-oxide	Owens et al suggested that both of oxidosqualene cyclase and lanosterol demethylase can be used as antiviral targets for HCV assembly.	(6)
lanosterol		
dimethylallyl-PP	Ye et al and Kapadia and Chisari reported the role of geranylgeranylation in HCV replication.	(7, 8)
farnesyl-PP		
geranyl-PP		
isopentenyl-pPP		
cholesterol	Takano et al and Rodgers et al downregulated the DHCR24 and DHCR7 genes to reduce HCV assembly.	(9, 10)
inositol	Bishé et al reviewed the role of phosphoinositides in the HCV assembly.	(11)
1D-myo-inositol-3-phosphate		
3-dehydrospinganine	Sakamoto et al downregulated the serine palmitoyltransferase gene to reduce HCV assembly.	(12)
sphinganine		
sn-glycerol-3-phosphate	Sn-glycerol-3-phosphate may prevent lipid biosynthesis through Kennedy pathway.	
1,2-diacylglycerol-LD-TAG pool (DAG)	Herker et al downregulated the DGAT1 gene to reduce HCV assembly.	(13)

# Omic Analysis

Condition 1

Condition 2

	P1	P2	...	Pm	N1	N2	N3	...	Nz	Fold Change	pvalue	Adjust pvalue
Gene1	1	1	1	1	10	10	10	10	10	=log2 average P / average N	t-test (P,N)	0.004
Gene 2	30	30	30	30	1	1	1	1	1			
Gene 3	20	20	20	20	19	19	19	19	19			
...												
Gene N												

# What is the biological meaning of these numbers

Genome



SRA file

```

> Read 1
AAAAATTTTAAA

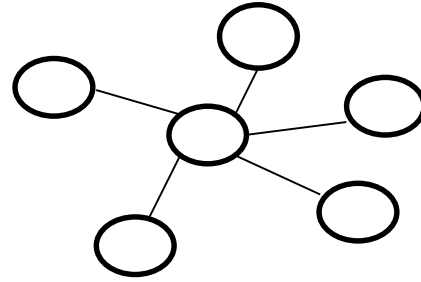
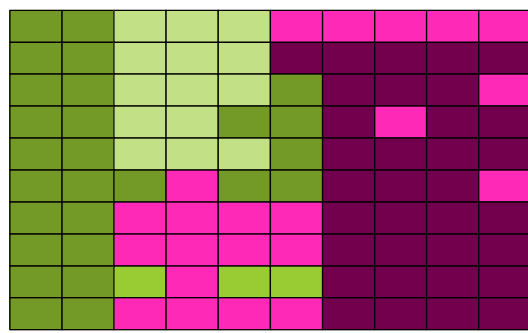
> Read 2
AAAACCCCCC

> Read 3
AAAACCCCCC

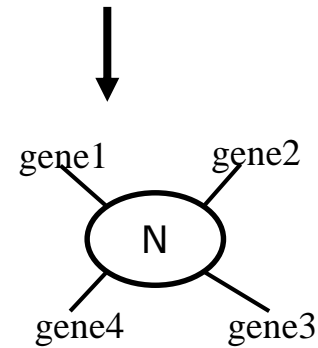
> Read 4
AAAACCCCCC
    
```

RNA-seq  
these numbers are number of reads

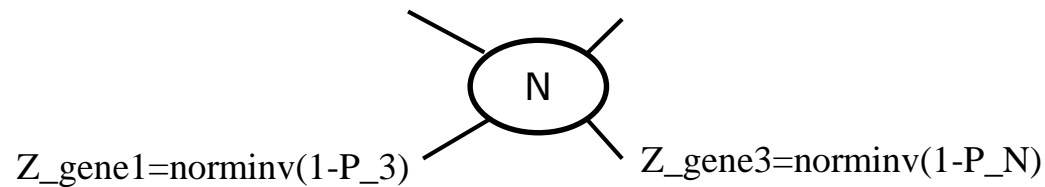
# Reporter Metabolites and Subnetworks



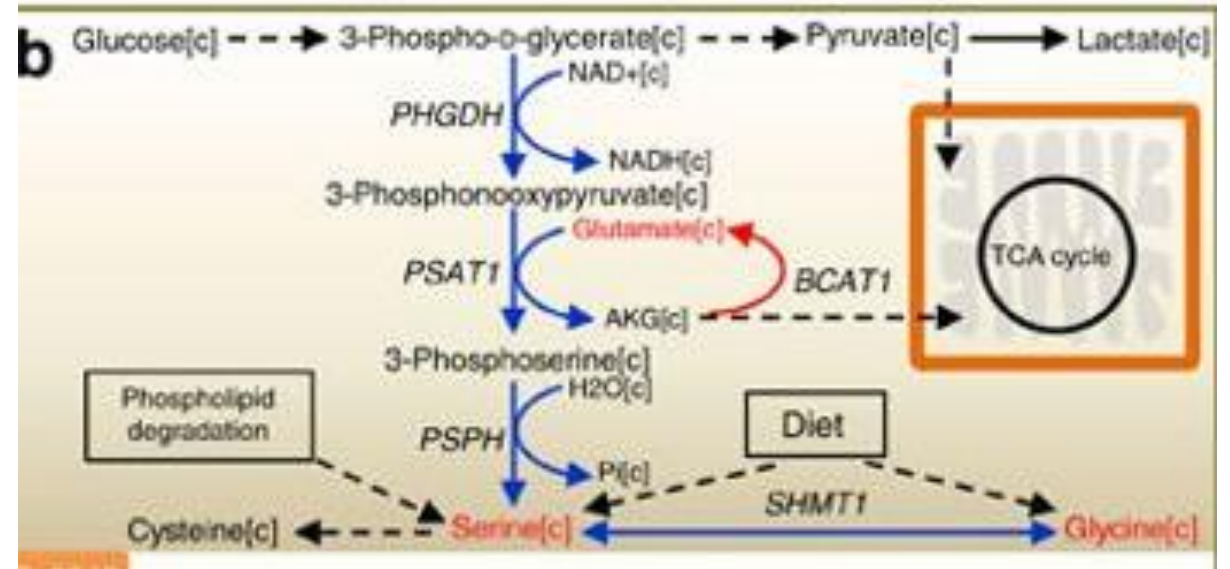
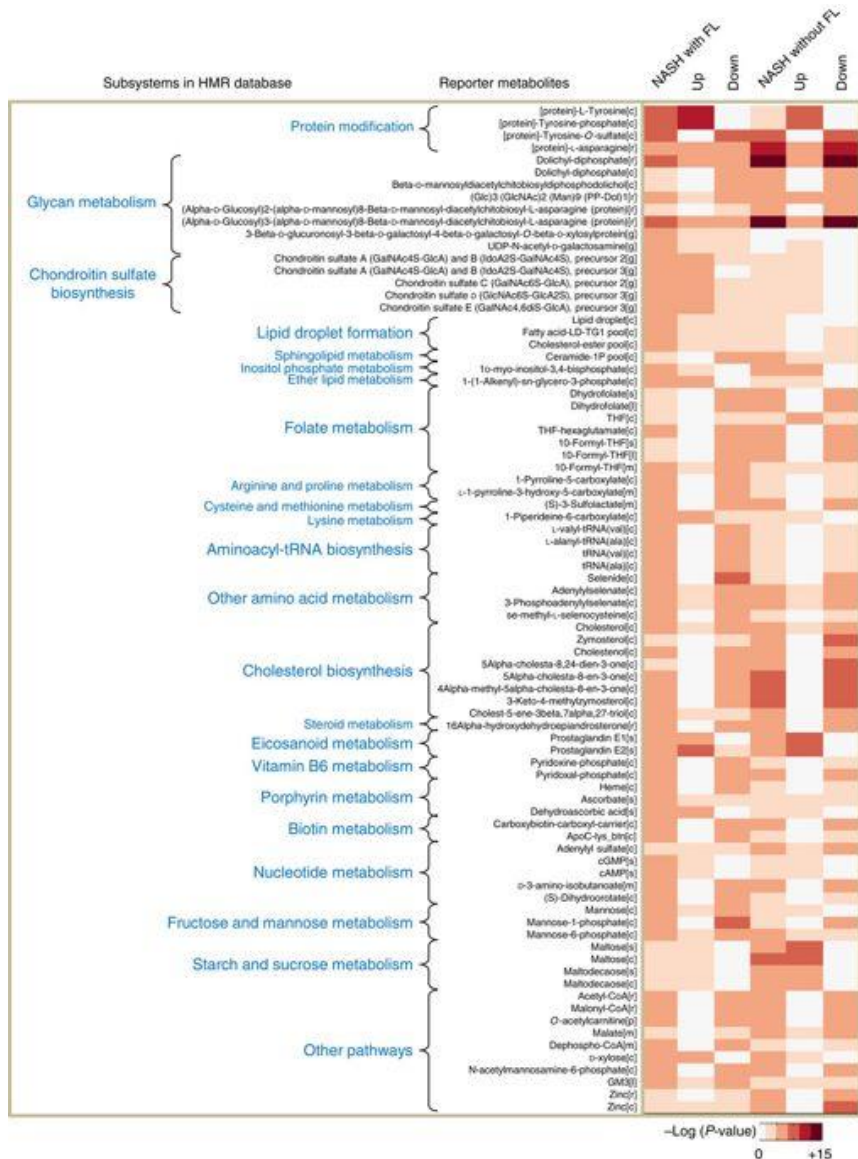
Gene	Adjust P. Value	Fold Change



$$Z_{\text{gene1}} = \text{norminv}(1-P_1) \quad Z_{\text{gene2}} = \text{norminv}(1-P_2)$$

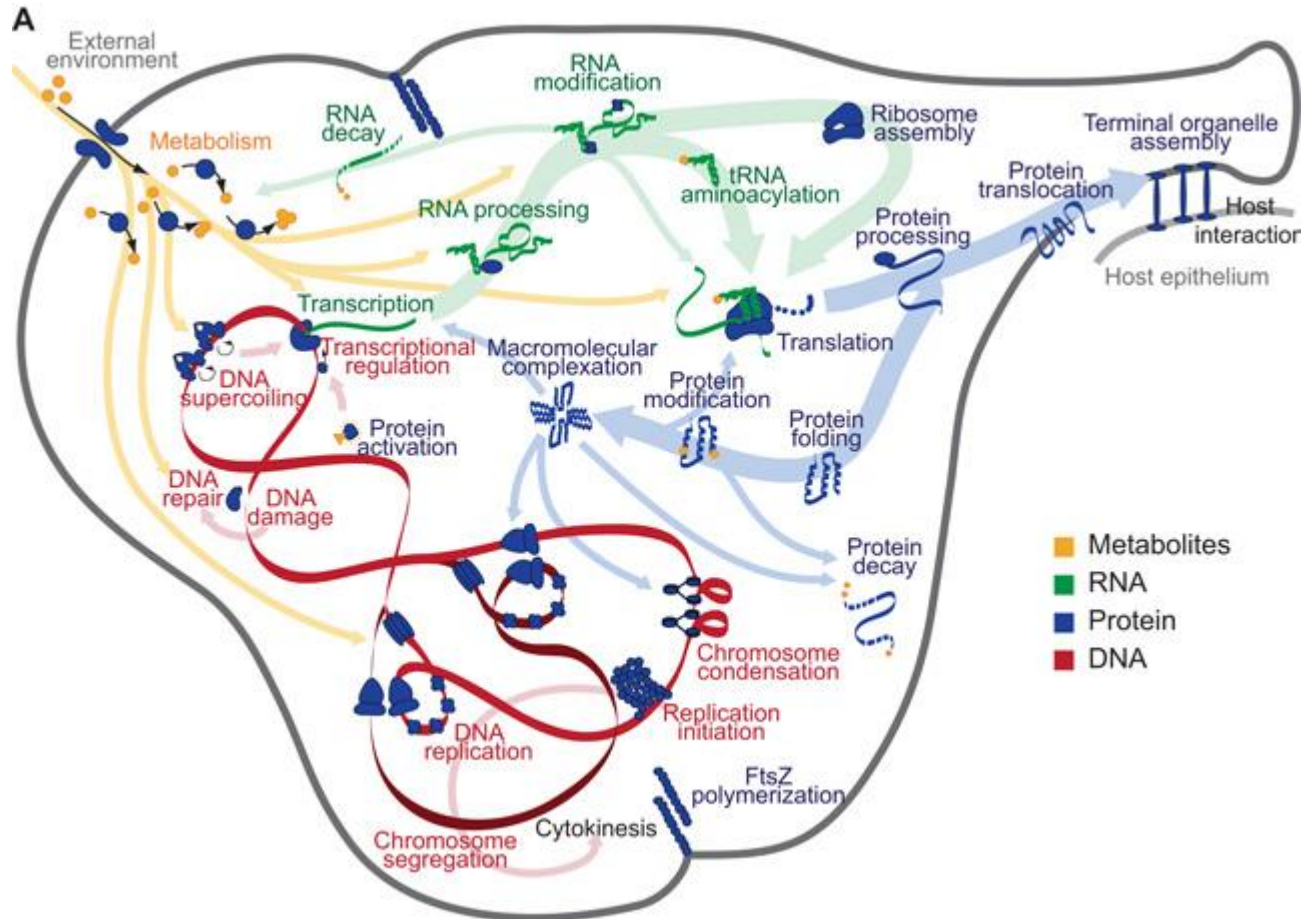


# Non-alcoholic fatty liver disease



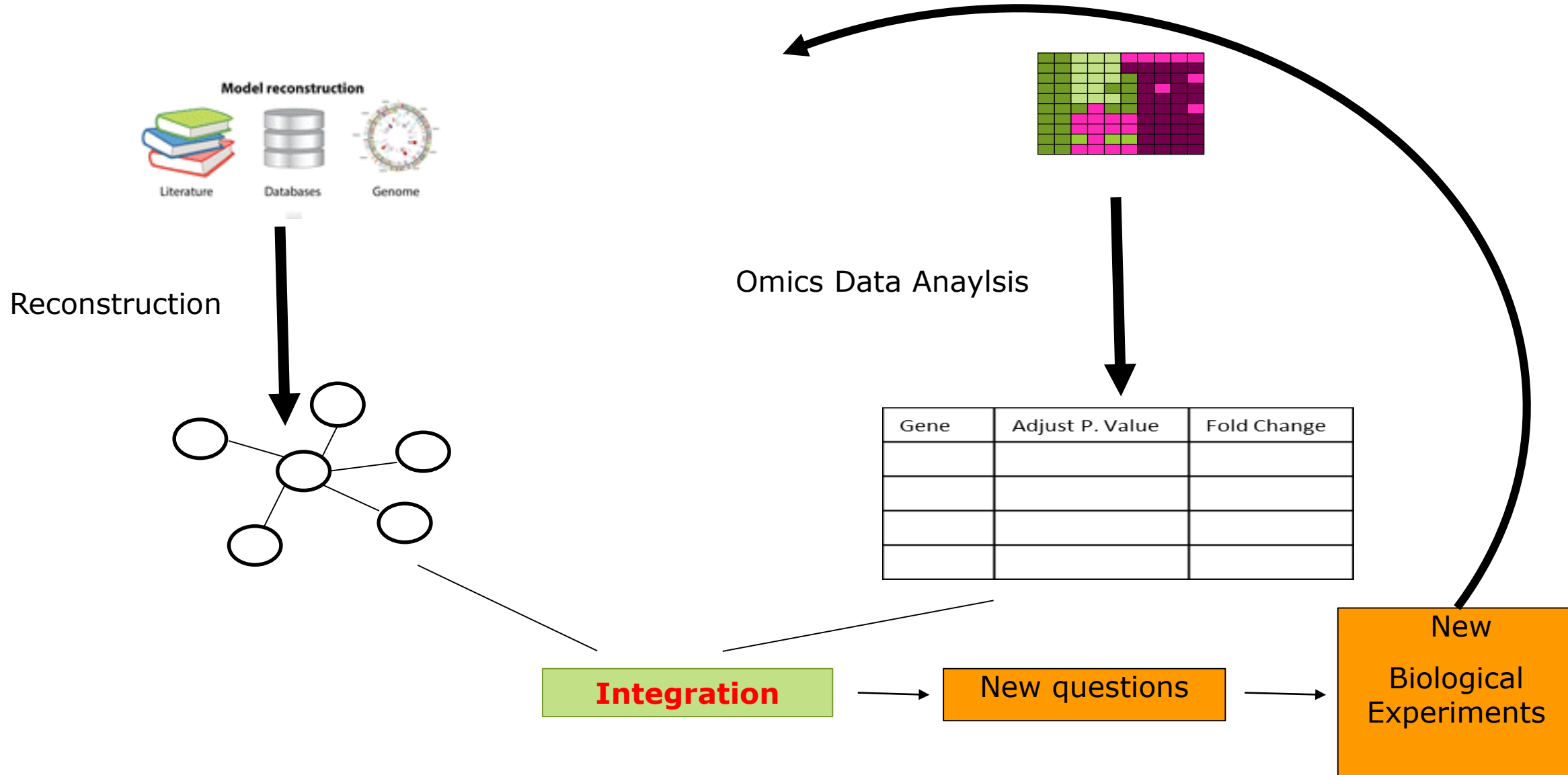
Nature Communications **volume5**, Article number: 3083 (2014)

# Whole Cell Modeling



[Cell. 2012 Jul 20; 150\(2\): 389–401.](#)

# Please Remember this Systems Biology Cycle



# Omics Data and tools

<https://cancergenome.nih.gov/>

<https://www.ebi.ac.uk/ena>

<https://galaxyproject.github.io/training-material/>

<http://kbase.us/>

# Genome-Scale Metabolic Models

<http://biomet-toolbox.chalmers.se/>

<http://www.metabolicatlas.com/>

<http://sbrg.ucsd.edu/optimizing-genres/>

<https://vmh.uni.lu/>

# More Free Courses

<https://www.youtube.com/watch?v=nHkYIEWNxeM>

<https://www.edx.org/course/case-studies-functional-genomics-harvardx-ph525-7x-0>

<https://www.video.ethz.ch/lectures/d-math/2014/spring/402-0112-14L/015a0d57-9372-4635-868c-342c0a1e61d6.html?autoplay=true>

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